Outline

1. Introduction

- * Electromagnetic solitary waves in plasmas: modeling & background
- * Rogue waves (freak waves) physical setting & preliminaries
- * Nonlinear amplitude modulation: basic phenomenology

2. Framework for EM wavepacket modulation

- * Multiscale perturbation technique
- * Evolution equation for the wavepacket envelope
- * Modulational (in)stability analysis
- 3. Electromagnetic (EM) rogue waves from first principles
- 4. Discussion & Summary

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3

Relativistic EM solitons

- *Relativistic solitons* are self-trapped, localized (finite-size) electromagnetic excitations of relativistic intensity that propagate without spreading due to diffraction.
- Dominant mechanisms are:
 - relativistic nonlinearity (relativistic mass variation)
 - striction nonlinearity (density perturbation due to ponderomotive effects)
 - * dispersion effects due to finite particle inertia.
- EM plasma solitons consist of electron (and ion) density depressions and intense electromagnetic field concentrations with a larger amplitude and a lower frequency than those of the laser pulse.
- EM energy localization!

Part 1: Intro #1 – Electromagnetic (EM) pulses in plasmas

- Old problem in relativistic electrodynamics in plasmas
 Akhiezer and Polovin (1956); Gerstein & Tzoar, PRL (1975); Marburger & Tooper, PRL (1975); Tsintsadze
 & Tskhakaya, JETP (1977), Kozlov, Litvak and Suvorov, JETP (1979)
- Recently gained impetus in the field of intense laser-plasma interaction:
 - * 1D theoretical investigations: Kaw, Sen and Katsouleas, PRL (1992); Kuehl, Zhang PRE (1993); Sudan et al, Phys. Plasmas (1997); Esirkepov et al., JETP Lett. (1998); Farina and Bulanov, PRL (2001); Farina and Bulanov, Plasma Phys. Rep., (2001); Hadzievski et al PoP (2002); Poornakala et al, PoP (2002); G. Lehmann, E.W. Laedke, K.H. Spatschek, PoP (2006); Lontano, Passoni, Bulanov, PoP (2003); Borhanian et al. PLA & PoP (2009); Sanchez-Arriaga et al, PoP (2011).
 - * PIC or fluid simulations: Bulanov et al., Plasma Phys. Rep. (1995); Bulanov et al., PRL (1999); Sentoku et al. Phys. Rev. Lett. (1999); Naumova et al., PRL (2001); Tushentsov et al, PRL (2001); Esirkepov et al, PRL (2002), Esirkepov et al, PRL (2004); Saxena et al, PoP (2006, 2007, 2013); Siminos et al, PRE (2014).
- Old problem in nonlinear physics: originally treated via reductive
 perturbation theory [Hasegawa, PRA (1970); Phys. Fluids (1972); Taniuti and co., JPSJ (1972)]

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4

Intro #2: Rogue waves - an emerging unifying concept

 Rogue waves are localized excitations (events) of extreme amplitude, exceeding twice the average strength of background turbulence level;



Data from the Draupner platform event in Norway (Jan. 1995). Credit: Kharif & Pelinovsky, Eur. Journal of Mechanics B/Fluids **22**, 603 (2003).





Fig. 1. Statistics of the super-carrier collision with rogue waves for 1968-1994.

Credit: Kharif & Pelinovsky, Eur. Journal of Mechanics B/Fluids 22, 603 (2003).

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5

7

Theoretical attempts to explain freak wave formation

... via water surface envelope mode interaction:



[Credit: M. Onorato, A.R. Osborne and M. Serio, Phys. Rev. Lett., 96 014503 (2006);
 P. K. Shukla, I. Kourakis, B. Eliasson, M. Marklund and L. Stenflo, Phys. Rev. Lett. 97, 094501 (2006);
 A. Grönlund, B. Eliasson and M. Marklund, EPL, 86 24001 (2009).]

Catastrophic encounters



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week ending 20 MAY 2011 8



Rogue Wave Observation in a Water Wave Tank

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[Credit: A. Chabchoub *et al*, Phys. Rev. Letters **106**, 204502 (2011); (right plot) A. Chabchoub/Hamburg University of Technology (online).]

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Analytical models for rogue waves

• Breather-type solutions of the *nonlinear Schrödinger (NLS) equation* were proposed by Dysthe & Trulsen (*) as possible analytical models for rogue waves.

Physica Scripta. Vol. T82, 48-52, 1999

Note on Breather Type Solutions of the NLS as Models for Freak-Waves

Kristian B. Dysthe¹ and Karsten Trulsen^{2†}

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[(*) K.B. Dysthe and K. Trulsen, Phys. Scripta T82, 48 (1999)]

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13

15

Roque waves in plasmas (2)

Rogue waves have been considered recently in various plasma contexts:

Alfvén-type rogue waves

[Shukla et al, Physics Letters A (2012)]

- Langmuir rogue waves in electron-positron plasmas [Moslem, PoP 2011]
- Electrostatic waves in e-p-i plasmas
 [El-Awady & Moslem, Phys. Plasmas 2011; El-Labany et al, Astrophys. Space Sci. 2012]
- Dusty plasmas

[Abdelsalam, et al, Phys. Plasmas 2011; Moslem et al, PRE 2011]

- Surface plasma waves [Moslem, Shukla and Eliasson, Europhys. Lett. 2011].
- Most of these studies have relied on a phenomenological analogy between rogue waves and large amplitude solutions of nonlinear model PDEs, e.g. KdV/mKdV or NLS equations (families).

Rogue waves in plasmas? (1)

- The rogue wave paradigm was recently employed in plasmas as a possible mechanism for magnetic hole generation (*).
- The generation of Alfvén type freak waves described by the *Derivative Nonlinear Schrödinger (DNLS)* equation was proposed (*).



[Electromagnetic Rogue Waves in Beam-Plasma Interactions, G.P. Veldes, J. Borhanian, M. McKerr, V. Saxena, D.J. Frantzeskakis and I. Kourakis, J. Optics **15** (Special issue on Optical Rogue Waves), 064003 (2013);

IoP LabTalk article (online, 2013): Monster waves in a laser beam: myth or reality?]





Intro: Prerequisites (continued)

The amplitude of a harmonic wave may vary in space and time:



This *modulation* (due to nonlinearity) may be *strong* enough to lead to wave *collapse* (modulational instability) or to the formation of *envelope solitons*:



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23

Part 2: Framework for EM wave modulation

Electron fluid-dynamical evolution equations + Maxwell laws:

$$\frac{\partial^2 \mathbf{A}}{\partial t^2} - \frac{\partial^2 \mathbf{A}}{\partial x^2} = \frac{\partial^2 \phi}{\partial t \partial x} \hat{x} + \frac{n}{\gamma} \mathbf{P},\tag{1}$$

$$\frac{\partial^2 \phi}{\partial x^2} = n - 1, \qquad \frac{\partial n}{\partial t} + \nabla(n\mathbf{V}) = 0,$$
 (2)

$$\frac{\partial(\mathbf{P} - \mathbf{A})}{\partial t} = \frac{\partial(\phi - \gamma)}{\partial x} \hat{x} + \mathbf{V} \times \nabla \times (\mathbf{P} - \mathbf{A}) - \mathbf{V} \times \mathbf{B}_0,$$
(3)

- A and ϕ are the vector and scalar potentials, respectively; $\mathbf{B}_{0} = \Omega \hat{x}$ is the ambient magnetic field.
- $V = P/\gamma$ is the fluid velocity (P is the electron momentum);
- γ is the relativistic factor $\gamma = \sqrt{1 + P^2}$.
- We have considered $\nabla \cdot = \frac{\partial \cdot}{\partial x} \hat{x};$
- ALL quantities are dimensionless; we have normalized:
 - * the scalar and vector potentials by mc^2/e , the electric field E by $mc\omega_{pe}/e$,
 - \star the magnetic field **B** by $m\omega_{pe}/e$,
 - \star the momentum by mc, the density by $n_{e,0}$, the electron velocity by the speed of light c.
- Space and time are scaled by the skin length c/ω_{p0} and the inverse plasma frequency ω_{p0}^{-1} .

[G. Lehmann et al, Phys. Plasmas 13, 092302 (2006); J. Borhanian et al, Phys. Lett. A 373, 3667 (2009).]

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(from: [Ya. Alpert, Phys. Reports 339, 323 (2001)])

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24

We set: $\mathbf{A} = A_y \hat{y} + A_z \hat{z}, \quad \mathbf{P} = P_y \hat{y} + P_z \hat{z} + \gamma u \hat{x}$ For CP EM pulses: $\mathbf{A}_1 = A_1(x, t)(\hat{y} + i\alpha \hat{z}), \mathbf{P}_1 = p_1(x, t)(\hat{y} + i\alpha \hat{z}) + \gamma u_1(x, t)$

• $p_{u,z}(x, t)$ and $\gamma u(x, t)$ denote the transverse and longitudinal component(s) of the electron momentum;

• $\alpha = +1$ ($\alpha = -1$) for left- (right-) hand circularly polarized electromagnetic (CPEM) waves.

The fluid-Maxwell system of equations then becomes

$$\frac{\partial^2 A_{y,z}}{\partial x^2} - \frac{\partial^2 A_{y,z}}{\partial t^2} = \frac{n}{\gamma} p_{y,z}, \qquad \frac{\partial^2 \phi}{\partial t \partial x} + nu = 0$$
(4)

$$\frac{\partial^2 \phi}{\partial x^2} = n - 1, \qquad \frac{\partial n}{\partial t} + \frac{\partial (nu)}{\partial x} = 0,$$
 (5)

$$\frac{\partial}{\partial t}(\gamma u) = \frac{\partial}{\partial x}(\phi - \gamma) + \frac{1}{\gamma} \left[p_y \frac{\partial}{\partial x}(p_y - A_y) + p_z \frac{\partial}{\partial x}(p_z - A_z) \right],\tag{6}$$

$$\frac{\partial}{\partial t}(p_{y,z} - A_{y,z}) + u\frac{\partial}{\partial x}(p_{y,z} - A_{y,z}) = \mp \Omega \frac{p_{z,y}}{\gamma} \qquad \left(\gamma = \sqrt{\frac{1+p^2}{1-u^2}}\right) \tag{7}$$

[Source(s): Kaw *et al*, PRL (1992); Esirkepov *et al*, JETP Lett. (1998); Poornakala *et al*, PoP (2002); Farina *et al*, PRL (2001).

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Multiscale perturbative technique for envelope dynamics

• Following the multiple scales (reductive perturbation) technique of Taniuti and coworkers (JMP & JPSJ 1969), we consider the stretched variables

 $\boldsymbol{X_n} = \boldsymbol{\epsilon}^n \boldsymbol{x} \; ; \quad \boldsymbol{T_n} = \boldsymbol{\epsilon}^n \boldsymbol{t} \; ; \qquad \boldsymbol{n} = 0, 1, 2, \dots$

- We define the state vector $\mathbf{S} = (n, u, p, \phi, A)$, and
- proceed by expanding near the equilibrium state $S^{(0)} = (1, 0, 0, 0, 0)$ as

$$\mathbf{S} = \mathbf{S}^{(0)} + \sum_{n=-\infty}^{n} \epsilon^n \mathbf{S}^{(n)}$$

where

$$\mathbf{S}^{(n)} = \sum_{l=-n}^{n} \mathbf{S}_{l}^{(n)} e^{il(kx-\omega t)}$$

denotes the amplitude of the *n*-th order contribution, as a series of the *l*-th harmonic amplitude(s) $\mathbf{S}_{(l)}^{(n)} = \mathbf{S}_{(l)}^{(n)}(X_j, T_j)$ (*slow*, for $j \ge 1$).

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27

- NLS equation for the vector potential (amplitude) $A_1^{(1)}$
- In order ~ ε³, an explicit compatibility condition is imposed for *annihilation* of secular terms (which would otherwise lead to a divergent solution).
- This analytical requirement can be expressed in the form

$$i\left(\frac{\partial A_1^{(1)}}{\partial T_2} + v_g \frac{\partial A_1^{(1)}}{\partial X_2}\right) + P \frac{\partial^2 A_1^{(1)}}{\partial X_1^2} + Q |A_1^{(1)}|^2 A_1^{(1)} = 0$$

• The dispersion coefficient *P* is given by

$$P = \frac{1}{2} \frac{d^2 \omega}{dk^2} = \frac{v_g}{2k} + \frac{v_g^2}{\omega - \alpha \Omega} - \frac{(3\omega - \alpha \Omega)v_g^3}{2k(\omega - \alpha \Omega)}.$$
 (8)

• The nonlinearity coefficient Q is

$$Q = \frac{v_g}{k} (\omega^2 - k^2)^4$$
 (9)

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Perturbative scheme – results

• The leading order system ($\sim \epsilon$) gives $\phi_1^{(1)} = n_1^{(1)} = u_1^{(1)} = 0$, along with:

$$(\omega^2 - k^2)A_1^{(1)} = p_1^{(1)}, \qquad \omega(p_1^{(1)} - A_1^{(1)}) = \alpha\Omega p_1^{(1)}$$

as expected [Hasegawa, Phys. Fluids 1972; Lehmann & Spatschek, Phys. Plasmas 2006].

• Dispersion relation:

$$\omega^2 - k^2 = \frac{\omega}{\omega - \alpha \Omega}$$

Here, α is +1/-1 for L-/R- CPEM waves (cf. book by Swanson 2003):



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28

Equilibrium solution & NL frequency shift

• The NLSE admits the harmonic wave solution for the electric potential amplitude :

$$\psi = \hat{\psi} e^{iQ|\hat{\psi}|^2\tau} + \text{c.c.}$$

• The total potential disturbance then reads:

$$\phi \simeq \epsilon \,\hat{\psi} e^{iQ|\psi|^2 \tau} \exp i(kx - \omega t) + \cdots$$

which takes the form

$$\phi \simeq \epsilon \hat{\psi} \exp i[kx - (\omega - \epsilon^2 Q |\hat{\psi}|^2) t] + \cdots$$

• the net result is a nonlinear frequency shift

$$\omega \rightarrow \omega - \epsilon^2 Q |\hat{\psi}|^2$$

which has been verified experimentally!

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• *Perturb* the amplitude by setting: $\hat{\psi} = \hat{\psi}_0 + \epsilon \hat{\psi}_{1,0} \cos{(\tilde{k}\zeta - \tilde{\omega}\tau)}$

• We obtain the (perturbation) dispersion relation:

 $\tilde{\omega}^2 = P^2 \tilde{k}^2 \left(\tilde{k}^2 - 2 \frac{Q}{P} |\hat{\psi}_{1,0}|^2 \right).$

Modulational (in)stability analysis

• If PQ < 0: the amplitude ψ is *stable* to external perturbations:



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31

- Localized envelope excitations (solitons)
- The NLSE accepts various solutions in the form: ψ = ρ e^{iΘ};
 the *total* electric potential is then: φ ≈ ε ρ cos(kr ωt + Θ)
 where the *amplitude* ρ and *phase correction* Θ depend on ζ, τ.
- Bright-type envelope soliton (pulse):



This is a propagating (and *oscillating*) localized pulse:

 $L = \sqrt{\frac{2P}{Q}} \frac{1}{\rho_0}$



- Modulational (in)stability analysis (continued...)
- If PQ > 0: the amplitude ψ is *unstable* for $\tilde{k} < \sqrt{2\frac{Q}{P}} |\psi_{1,0}|$.



- Maximum (instability) growth rate: $\sigma = Q |\psi_{1,0}|^2$, occurs at $\tilde{k}_m < \sqrt{\frac{Q}{P}} |\psi_{1,0}|$
- Instability occurs in the "window": $0 < \tilde{k} < \sqrt{2 \frac{Q}{P}} |\psi_{1,0}|$.
- The wave may either "blow up", or localize its energy towards the formation of (envelope) solitons.

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32







Localized envelope excitations

• Dark-type envelope solution (*hole soliton*):

$$\rho = \pm \rho_1 \left[1 - \operatorname{sech}^2 \left(\frac{\zeta - v\tau}{L'} \right) \right]^{1/2} = \pm \rho_1 \tanh \left(\frac{\zeta - v\tau}{L'} \right)$$
$$\Theta = \frac{1}{2P} \left[v \zeta - \left(\frac{1}{2} v^2 - 2PQ\rho_1^2 \right) \tau \right]$$
$$L' = \sqrt{2 \left| \frac{P}{Q} \right|} \frac{1}{\rho_1}$$

This is a propagating localized hole (zero density void):



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39

- Localized envelope excitations
- Grey-type envelope solution (void soliton):

This is a

void:

propagating



40

Envelope solitons in action (2): anomalous vs. normal dispersion Bright envelope solitons on the space-time plane: stable vs unstable:



Dark-type envelope solitons on the space-time plane: stable vs unstable:



[Numerical results by Sharmin Sultana, Queen's University Belfast.]

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38

Envelope solitons in action (1): anomalous vs. normal dispersion

Case PQ > 0 ("Anomalous dispersion"): stable bright (left plot)/ unstable dark (right plot) envelopes:



Case PQ < 0 ("Normal dispersion"): unstable bright (left plot) / stable dark (right plot) envelopes:



[Numerical results by Sharmin Sultana, Queen's University Belfast.]

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Modulational (in)stability: parametric dependence on Ω

The magnetic field may either *enhance MI* (LCP, $\Omega < \omega_{p,e}$; top left plot) or -generally- *suppress MI* (reduced growth rate for higher Ω).



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43

Variation of P/Q with ω (for variable Ω)

- PQ < 0 (wavepackets stable) for low ω ; MI above threshold ω_{cr}
- L- CPEM: Lower instability threshold for weakly magnetized plasma (ω_c < ω_p); higher for strongly magnetized plasma (ω_c > ω_p)
- R- CPEM: Instability threshold practically stable, but strong dependence of P/Q ratio (\rightarrow soliton width) on Ω .



[G. Veldes, J. Borhanian, V. Saxena, D. Franzeskakis and I. Kourakis, in preparation (2013)]

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Peregrine Soliton as a model for rogue waves

• As a first approach to rogue waves, we consider the Peregrine soliton:

$$\psi(\xi,\tau) = \left[1 - \frac{4(1+i2Q\tau)}{1+2Q\xi^2/P + 4Q^2\tau^2}\right] \exp\left(iQ\tau\right)$$

[D. H. Peregrine, J. Austral. Math. Soc. B **25**, 16 (1983); K. B. Dysthe & K. Trulsen, Physica Scripta **T82**, 48 (1999); V. I. Shrira & V. V. Geogjaev, J. Eng. Math. **67**, 11 (2010); B. Kibler, *et al.*, Nat. Phys. **6**, 790 (2010)]

- The Peregrine paradigm as a prototypical model for rogue waves has recently been employed successfully in NL optics [Kibler *et al*, Nat. Phys. (2010)];
- Recalling the functional dependence of P and Q on plasma parameters, this model allows one to investigate the parametric dependence on the magnetic field Ω and wavenumber k (reduced variables).
- Ab initio analytical predictions, numerical confirmation.

42

Part 3: Analytical models for rogue waves

Various solutions of the NLS equation have been proposed as model candidates for rogue waves.

We distinguish:

• The Peregrine soliton

[D. H. Peregrine, J. Austral. Math. Soc. B **25**, 16 (1983); K. B. Dysthe, and K. Trulsen, Physica Scripta **T82**, 48 (1999); V. I. Shrira, and V. V. Geogjaev, J. Eng. Math. **67**, 11 (2010); B. Kibler, J. Fatome, et al., Nature Physics **6**, 790 (2010)]

• The Kuznetsov-Ma breather

[Ya C. Ma, Stud. Appl. Math. 60, 43 (1979)];

• The Akhmediev breather

[N. N. Akhmediev, V. M. Eleonskii, and N. E. Kulagin, Theor. Math. Phys. 72, 809 (1987)];

In the following, we have considered the above paradigms, with an aim to investigate their dependence on relevant plasma parameters (Ω in particular).



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[Figure from: Kibler et al, Nat. Phys. (2010) & Nature/Sci.Rep. (2012).]

Time τ

-2

Distance &

-5



51

Parametric analysis (1- LCP/low frequency)

- Rogon management/tuning by the magnetic field (via $\Omega = \omega_c/\omega_n$);
- The magnetic field suppresses the spatial extension of breathers, and
- ... reduces the time duration in all 3 cases.







[G. Veldes, J. Borhanian, V. Saxena, D.J. Frantzeskakis and I. Kourakis, to appear in J. Optics (IoP) (2013).]

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Parametric analysis (2- LCP/high frequency)

- Rogon management/tuning by the magnetic field (via $\Omega = \omega_c / \omega_n$);
- The magnetic field suppresses the spatial extension of breathers, and
- ... reduces the time duration in all 3 cases.



[G. Veldes, J. Borhanian, V. Saxena, D.J. Frantzeskakis and I. Kourakis, to appear in J. Optics (IoP) (2013).]

52



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55





[[]V. Saxena, J. Kourakis, G. Sanchez-Arriaga, E. Siminos, Phys. Lett. A, 377, 473 (2013).]

Conclusions & Summary

- Multiscale methodology for EM relativistic solitons revisited
- Powerful analytical technique, provides predictions for
 - Modulational Instability thresholds and growth rate
 - Envelope modes, harmonic generation, rogue waves
- Efficient analytical toolbox for Rogue Waves in laser-plasma interactions
- *Rogue waves* are random events, may be tedious to detect experimentally;
- Results to be compared with large-amplitude theory (e.g., Kaw-Sen-Katsouleas or Farina-Bulanov formalism)
- Static predictions so far; need for dynamical (numerical) investigation.
- Work in progress: fluid simulations, PIC simulations, higher-order breathers, ...

54

56

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