

## Modulational Instability Of Dust Electron Acoustic Waves In Superthermal Dusty Plasmas

N. S. Saini, S. Sultana, and I. Kourakis

Citation: *AIP Conf. Proc.* **1397**, 355 (2011); doi: 10.1063/1.3659840

View online: <http://dx.doi.org/10.1063/1.3659840>

View Table of Contents: <http://proceedings.aip.org/dbt/dbt.jsp?KEY=APCPCS&Volume=1397&Issue=1>

Published by the [American Institute of Physics](#).

---

### Related Articles

Non-resonant parametric amplification in biomimetic hair flow sensors: Selective gain and tunable filtering  
*Appl. Phys. Lett.* **99**, 213503 (2011)

The effect of electrostatic shielding using invisibility cloak  
*AIP Advances* **1**, 042126 (2011)

A molecular Debye-Hückel theory and its applications to electrolyte solutions  
*J. Chem. Phys.* **135**, 104104 (2011)

Adhesion selectivity by electrostatic complementarity. I. One-dimensional stripes of charge  
*J. Appl. Phys.* **110**, 054902 (2011)

Quantitative potential measurements of nanoparticles with different surface charges in liquid by open-loop electric potential microscopy  
*J. Appl. Phys.* **110**, 044315 (2011)

---

### Additional information on AIP Conf. Proc.

Journal Homepage: <http://proceedings.aip.org/>

Journal Information: [http://proceedings.aip.org/about/about\\_the\\_proceedings](http://proceedings.aip.org/about/about_the_proceedings)

Top downloads: [http://proceedings.aip.org/dbt/most\\_downloaded.jsp?KEY=APCPCS](http://proceedings.aip.org/dbt/most_downloaded.jsp?KEY=APCPCS)

Information for Authors: [http://proceedings.aip.org/authors/information\\_for\\_authors](http://proceedings.aip.org/authors/information_for_authors)

### ADVERTISEMENT



**AIP**Advances

*Submit Now*

**Explore AIP's new  
open-access journal**

- **Article-level metrics  
now available**
- **Join the conversation!  
Rate & comment on articles**

# Modulational Instability Of Dust Electron Acoustic Waves In Superthermal Dusty Plasmas

N. S. Saini\*, S. Sultana<sup>†</sup> and I. Kourakis<sup>†</sup>

\*Department of Physics, Guru Nanak Dev University, Amritsar, India  
nssaini@yahoo.com

<sup>†</sup>Centre for Plasma Physics, Queen's University Belfast, BT7 1 NN, Northern Ireland, UK

**Abstract.** In this investigation we have studied how dust concentration and superthermality of electrons affect the instability growth rate of dust electron-acoustic waves. Both type of dark and bright envelope solitons are observed.

**Keywords:** Instability, superthermal, envelope solitons, electron-acoustic wave.

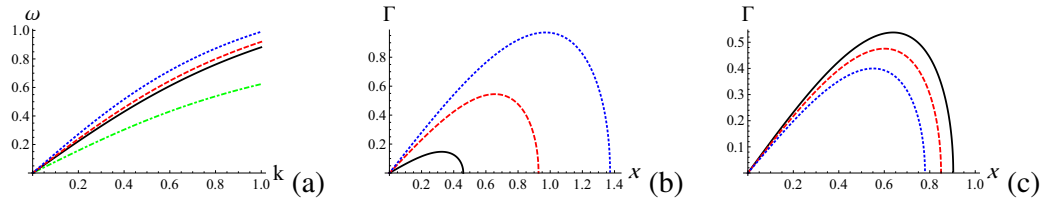
**PACS:** 52.27.Lw, 05.45.Yv, 52.35.Sb

Electron-acoustic waves (EAWs) having high frequency occur in plasmas are characterized by two type populations of electrons (namely, cold and hot electrons). A large number of investigations have been reported to study the characteristics of EAWs in an unmagnetized plasmas [1, 2]. Dust particles are ubiquitous component of space and astrophysical environments and their presence in a plasma has long been shown theoretically and confirmed experimentally to generate new modes [3], and also to modify the characteristics of existing ones, including the electron-acoustic (EA) mode [4, 5]. A kappa type distribution function [6] is most appropriate to model effectively the excess superthermality phenomenon. Over the last years, the study of the modulational instability (MI) of solitary waves has been a field of great interest in various plasma situations [7, 8]. Very recently, Sharmin and Kourakis [9] have studied modulational instability (MI) of electron-acoustic solitary waves in the presence of excess superthermality of electrons. Our aim is to investigate the nonlinear self-modulation of electron-acoustic waves in the presence of dust particles and excess superthermal electrons.

We adopt a fluid model, following the formalism in [9], by adding a dust species in the background. The latter affects the charge balance through Poisson's equation; investigating this effect is our scope in this brief communication. From charge neutrality at equilibrium,  $n_{c0}/n_{h0} = Z_i n_{i0}/n_{h0} + s Z_d n_{d0}/n_{h0} - 1 = \alpha$ . A multiple scales perturbation technique [10] is used to study the dynamics of a slowly-varying amplitude of electrostatic excitations. Details on the technique are given in Ref. [9], only final expressions are provided in this manuscript. From the first order evolution equations, we obtain the dispersion relation as  $\omega^2 = k^2 \alpha / (k^2 + c_1)$ .

The tedious calculation will be reported in a more detailed account of our work; the long expression for the coefficient Q is omitted here. The dispersion coefficient  $P = -\frac{3}{2} \frac{\omega^5 c_1}{k^4 \alpha^2}$ , which is a negative quantity. The expression for the nonlinearity coefficient Q, due to the carrier wave self-interaction in the background plasma is same as given in Ref. [9], by replacing  $\beta$  with  $\alpha$ . For lack of space, we limit ourselves here to providing a brief account of our main results below. We obtain a nonlinear Schrödinger

(NLS) equation, identical in structure to Eq. (19) in Ref. [9], yet now incorporating the influence of the dust presence. The expression for the growth rate identical to Eq. (27) in Ref. [9] with  $\Gamma = \tilde{\omega}/(Q_\infty|\psi_0|^2)$  and  $x = \tilde{k}/(Q_\infty/P_\infty)^{1/2}|\psi_0|$  with  $P_\infty = P(\kappa \rightarrow \infty)$  and  $Q_\infty = Q(\kappa \rightarrow \infty)$  is used to investigate the instability's dependence on superthermality (via  $\kappa$ ) and dust concentration (via  $\alpha$ ). Figure (a) shows the variation of  $\omega$  with the wave number  $k$  for different values of  $\kappa$  as well as dust concentration.  $\omega$  decreases as the value of  $\kappa$  increases. Figs. (b) and (c) show the variation of the modulational instability (MI) growth rate with the effects of excess superthermality (via  $\kappa$ ) and negative dust concentration (via  $\alpha$ ) respectively. The MI growth rate decreases with increase in superthermality as well as dust concentration. The threshold  $k_{cr}$  separates the stable region(s) ( $k < k_{cr}$  or  $P/Q < 0$ ) from the unstable one(s) ( $k > k_{cr}$  or  $P/Q > 0$ ). We have also observed that critical wave number  $k_{cr}$  where instability sets in increases with increase in superthermality as well as negative dust concentration. The exact results of Ref. [9] are recovered in the absence of charged dust. Further, with no dust, for a very large value of  $\kappa$ , the results of Ref. [7] are well recovered. It is concluded that bright and dark-type envelope structures are observed and their characteristics are modified by the superthermality of electrons and dust concentration.



**FIGURE 1.** The variation of the frequency  $\omega$  with wave number  $k$  (for different values of  $\kappa$  and dust concentration; dot-dashed: no dust; with dust, solid:  $\kappa = 3.25$ , dashed:  $\kappa = 4.25$ , Dotted:  $\kappa = 25$ ) and growth rate  $\Gamma$  for different values of (b) superthermality parameter (solid:  $\kappa = 3.25$ , dashed:  $\kappa = 4.25$ , Dotted:  $\kappa = 25$ ) and (c) dust concentration (solid  $\mu_d = 0.2$ , dashed:  $\mu_d = 0.25$ , Dotted:  $\mu_d = 0.3$ ).

## REFERENCES

1. R. Pottelette et al., Geophys. Res. Lett. **26**, 2629 (1999).
2. N. Dubouloz, R. A. Treumann, R. Pottelette and, M. Malingre, J. Geophys. Res. **98**, 17415 (1993); R. L. Mace, et al., J. Plasma Phys. **45**, 323 (1991); M. Berthomier, et al., Phys. Plasma **7**, 2987 (2000).
3. P. K. Shukla and A. A. Mamun, *Introduction to Dusty Plasma Physics* (IOP, Bristol, 2002).
4. M. Y. Yu and P. K. Shukla, J. Plasma Phys. **29**, 409-413 (1983); R. L. Tokar and S. P. Gary, Geophys. Res. Lett. **11**, 1180-1183 (1984)
5. J. Vranjes, H. Saleem and S. Poedts, Planetary and Space Science **50**, 807-810 (2002)
6. V. M. Vasyliunas, J. Geophys. Res. **73**, 2839-2884 (1968).
7. I. Kourakis and P. K. Shukla, Phys. Rev. E **69**, 036411 (2004)
8. I. Kourakis and P. K. Shukla, Nonlin. Proc. Geophys. **12**, 407 (2005).
9. S. Sultana and I. Kourakis, Plasma Phys. Cont. Fusion **53**, 045003 (2011).
10. T. Taniuti and N. Yajima, J. Math. Phys. **10**, 1369 (1969).